

20.110/2.772 Fall 2005

Recitations 3-4  
Week of Sep 20

1. State functions: An ideal gas is initially at the following conditions:  $V = 1 \text{ L}$ ,  $P = 1 \text{ atm}$ ,  $T = 298\text{K}$  (State 0). It is subjected to the following cycle, where each step between states is reversible:

- Step 1: Isothermal expansion to 2 L (State 1)
- Step 2: Adiabatic expansion to 3 L (State 2)
- Step 3: Isothermal compression to 1.5 L (State 3)
- Step 4: Adiabatic compression to 1 L (State 0)

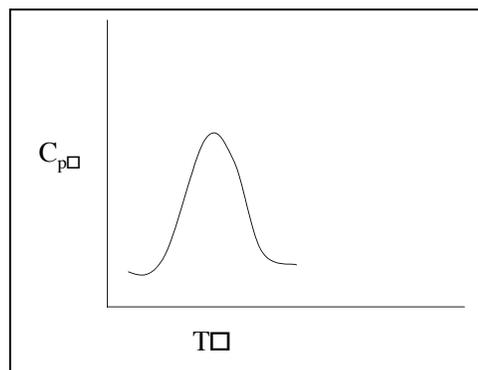
Calculate the heat, work, and change in internal energy for the gas at each step. For one complete round of the cycle, what is the net value of  $q$ ? the net value of  $w$ ? the net value of  $\Delta U$ ?

2. Heat of Unfolding of a Protein: Proteins in solution are folded into 3D structures that are stabilized by many non-covalent bonds between the amino acids. As the temperature of a protein solution increases, these bonds become less stable and the protein undergoes a denaturation process where it unfolds and interacts more with water. The enthalpy of this reaction can be measured by microcalorimetry at constant pressure, where the value  $C_{p, \text{protein}} = (\partial H / \partial T)_p$  for a dilute solution is determined relative to the solvent and as a function of temperature. A typical set of experimental data is shown in the figure.

Privalov and coworkers<sup>1</sup> have measured determined  $C_p(T)$  for the protein lysozyme and found the data for one of the domains fit the following form, where  $\Delta C_p$  is relative to the solvent

$$\Delta C_p = \Delta C_p(T_i) + b(T - T_i) + c(T^2 - T_i^2)$$

In this expression,  $T_i$  refers to the temperature at the peak of the transition, and all temperatures are in K. Determine the enthalpy of denaturation of lysozyme if  $T_i = 41.5^\circ\text{C}$ ,  $b = 0.3158 \text{ J/K}^2\text{-mol}$  and  $c = 0.462 \times 10^{-3} \text{ J/K}^3\text{-mol}$ . The temperature range for the transition is  $20\text{-}60^\circ\text{C}$ .



<sup>1</sup> Y.V. Griko, E. Friere, G. Privalov, H. van Dael, P.L. Privalov, J. Mol. Biol., 252, 447-459 (1995)