

## Quiz No. 1

Monday, October 25, 2004

This is a CLOSED-BOOK, open-notes Quiz.

**Problem 1** (20 points)

Servomotors make the flywheel spin at a constant rate  $\omega_2$ , and also impose a vertical rotation rate  $\omega_1$  that is a function of time (see figure below). The center of mass of the flywheel is located on the  $z$  axis, and the centroidal moments of inertia are  $I_1$  about the spin axis and  $I_2$  transverse to that axis.

- Derive the equations of motion for the system.
- Determine the external torques necessary to maintain the above motion.

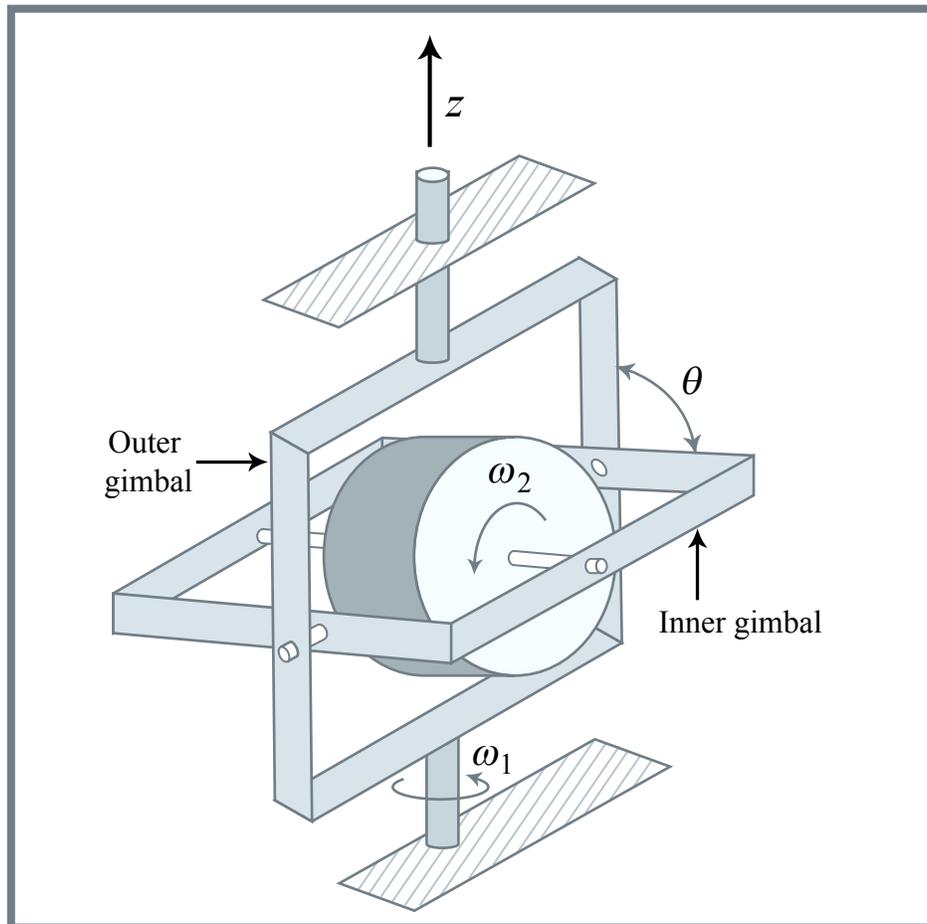


Figure by OCW.

**Problem 2** (20 points)

A solid uniform cylinder of mass  $m$  and radius  $R$  is placed on top of a fixed cylinder of the same radius, and it is slightly tipped, as shown in the figure. Find the value of the angle  $\theta$  at which sliding begins as a function of the static friction coefficient  $\mu$ .

