R16

[5+5]

Code No: 133BC JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD B.Tech II Year I Semester Examinations, April/May - 2018 MATHEMATICAL FOUNDATIONS OF COMPUTER SCIENCE (Common to CSE, IT) Max. Marks: 75 Time: 3 Hours Note: This question paper contains two parts A and B. Part A is compulsory which carries 25 marks. Answer all questions in Part A. Part B consists of 5 Units. Answer any one full question from each unit. Each question carries 10 marks and may have a, b, c as sub questions. PART-A (25 Marks) Construct the truth table for the following formula: 1.a) [2] $\neg (P \lor (Q \land R)) \longleftrightarrow ((P \lor Q) \land (P \lor R))$ [3] Explain duality law. b) Give the formal definition for the composition of binary relations. [2] c) 131 What are the properties of a group? d) State addition principle and give an example of a problem solved by addition principle. e) [2] [3] State pigeon-hole principle. f) [2] What is the general form of a first-order recurrence relation? g) What is the generating function of 1.-1,1,-1,... 131 h) If a simple graph G contains n vertices and m edges, how many number of edges are i) [2] present in Graph G' (complement of G). How many edges are present in a complete graph with n vertices? Explain. [3] PART-B (50 Marks) Show the following equivalence without constructing the truth table. 2.a) $((P \land Q \land A) \to C) \land (A \to (P \lor Q \lor C)) \Leftrightarrow (A \land (P \leftrightarrow Q)) \to C$ Without constructing a truth table, show that $A \wedge E$ is not a valid consequence of b) [5+5] $A \leftrightarrow B \quad B \leftrightarrow (C \land D) \quad C \leftrightarrow (A \lor E) \quad A \lor E$ OR Obtain the principal disjunctive and conjunctive normal form of the following formula. 3.a) $(P \to (Q \land R)) \land (\neg P \to (\neg Q \land \neg R))$ For the following formulas, let the universe be R. Translate each of the following sentences into a formula (using quantifiers): i) There is a smallest number. (ii) Every positive number has a square root. (Do not use the square root symbol: use only



multiplication.)

- 4.a) Consider the following Hasse diagram of a partially ordered set $\langle P, R \rangle$, where $P = \{x_1, x_2, x_3, x_4, x_5\}$. Find the least and greatest members in P if they exist. Also find the maximal and minimal elements of P. Find the upper and lower bounds of $\{x_2, x_3, x_4\}$, $\{x_2, x_4, x_5\}$ and $\{x_1, x_2, x_3\}$. Also indicate the LUB and GLB of these subsets if they exist.
 - b) Let $n \in N^+$ and $G_1, G_2, ..., G_n$ be groups, and consider $\prod_{i=1}^n G_i := G_1 \times G_2 \times ... \times G_n = \{(a_1, a_2, ..., a_n) : a_i \in G_i \forall i = 1, 2, ..., n\} \text{ with the operation } \dagger$ where if $x = (a_1, a_2, ..., a_n)$ and $y = (b_1, b_2, ..., b_n)$, then $x \dagger y = (a_1b_1, a_2b_2, ..., a_nb_n)$, where each product a_ib_i is performed according to the operation of the group G_i . Show that $\prod_{i=1}^n G_i$ is a group.

OR

- 5.a) Find the transitive closure of the relation $R = \{(1,2), (2,3), (3,4), (4,1)\}$. Show R' for all values of i that give new elements of the transitive closure.
- b) Find all the subgroups of (i) $(Z_{12}, +_{12})$; and (ii) (Z_7, \times_7) . [5+5]
- 6. In the United States and Canada, a telephone number is a 10-digit number of the form NXX NXX XXXX where $N \in \{2,3,...9\}$ and $X \in \{0.1,2,....9\}$. How many telephone numbers are possible? The first three digits of a telephone number are called an area code. How many different area codes must a city with 23.000.000 phones have? A previous scheme for forming a telephone numbers required a format of NYX NXX XXXX where N and X are defined as above and Y is either a 0 or a 1. How many more phone numbers are possible under the new format than under the old format?

OR

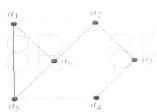
- 7.a) How many four letter words can be formed using the letters a, a, a, b, b, c, c, c, c, d, d?
- b) Expand $(2x y)^7$ using the Binomial Theorem. [5+5]
- 8.a) Solve the recurrence relation $a_n = 2a_{n-1} + 3a_{n-2}$ for $n \ge 2$ where $a_0 = 2$ and $a_1 = 2$.
 - b) Using generating function find a_n in terms of n if $a_0 = 1$, $a_1 = 2$ and $a_{n+2} = 5a_{n+1} 4a_n$ for $n \ge 0$.

OR

- 9.a) Solve the recurrence relation $T(n) = 4T(n-1) + 2^n$, with T(0) = 6.
- b) Find the coefficient of x^{2005} in the generating function $\frac{1}{(1+5x)^2}$. [5+5]

10.a) Determine whether the given pair of graphs is isomorphic?

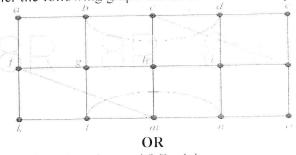






Determine whether the following graph has an Euler circuit or path.

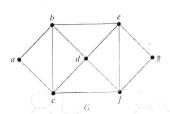
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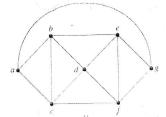


11.a)

[5+5]

How do you test the planarity of a graph? Explain. What are the chromatic numbers of the graph G and H?





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